

# Blind Super-Resolution

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*\* Joint work with Tomer Michaeli [ICCV 2013]*

# Super-Resolution

- *Classical multi-image SR*
- *Example-based SR*
  - *External*
  - *Internal*

**Wrong blur kernel**

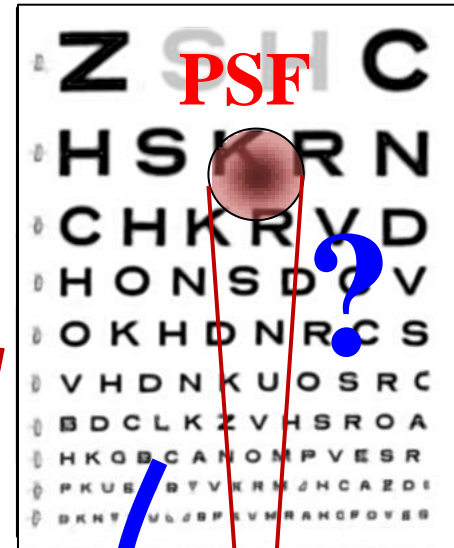
**→ Bad SR results**

Blind Super Resolution

In this work:

1. The correct blur  $k$  is NOT the *PSF*
2. Recover the optimal SR kernel  $k$  directly from the low-res image  $l$

high-res image  $h$

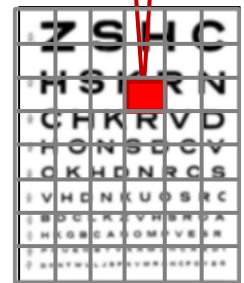


Assumed known

$$(h * k) \downarrow \alpha$$

*PSF*  
*Gaussian*

⋮



low-res image  $l$

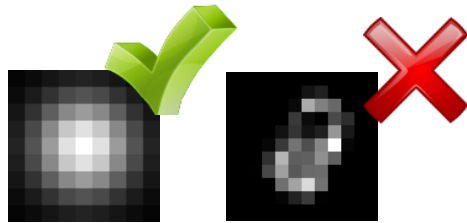
# Prior Work on Blind-SR

- **Parametric kernels:**

*[Begin & Ferrie. '04], [Wang et al. '05], [Qiao et al. '06], [He et al. '09]*

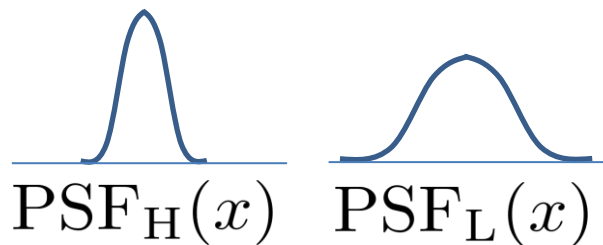
- **Nonparametric kernels with a single peak:**

*[Joshi et al. '08]*



**Our goal: General Nonparametric Blind-SR**

# What is the Correct Blur Kernel?



continuous scene  $f(x)$



PSF<sub>H</sub>( $x$ )

high-res PSF

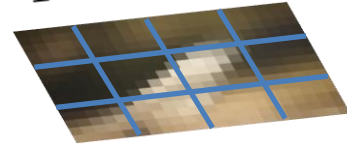
high-res image  $h[n]$



PSF<sub>L</sub>( $x$ )

low-res PSF

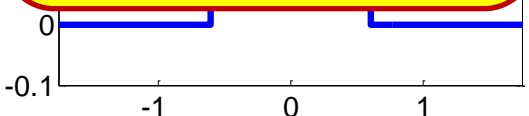
low-res image  $l[n]$



$(*k[n]) \downarrow \alpha$

**Intuitively:**

$$K(\omega) = \frac{\mathcal{PSF}_L(\omega)}{\mathcal{PSF}_H(\omega)}$$



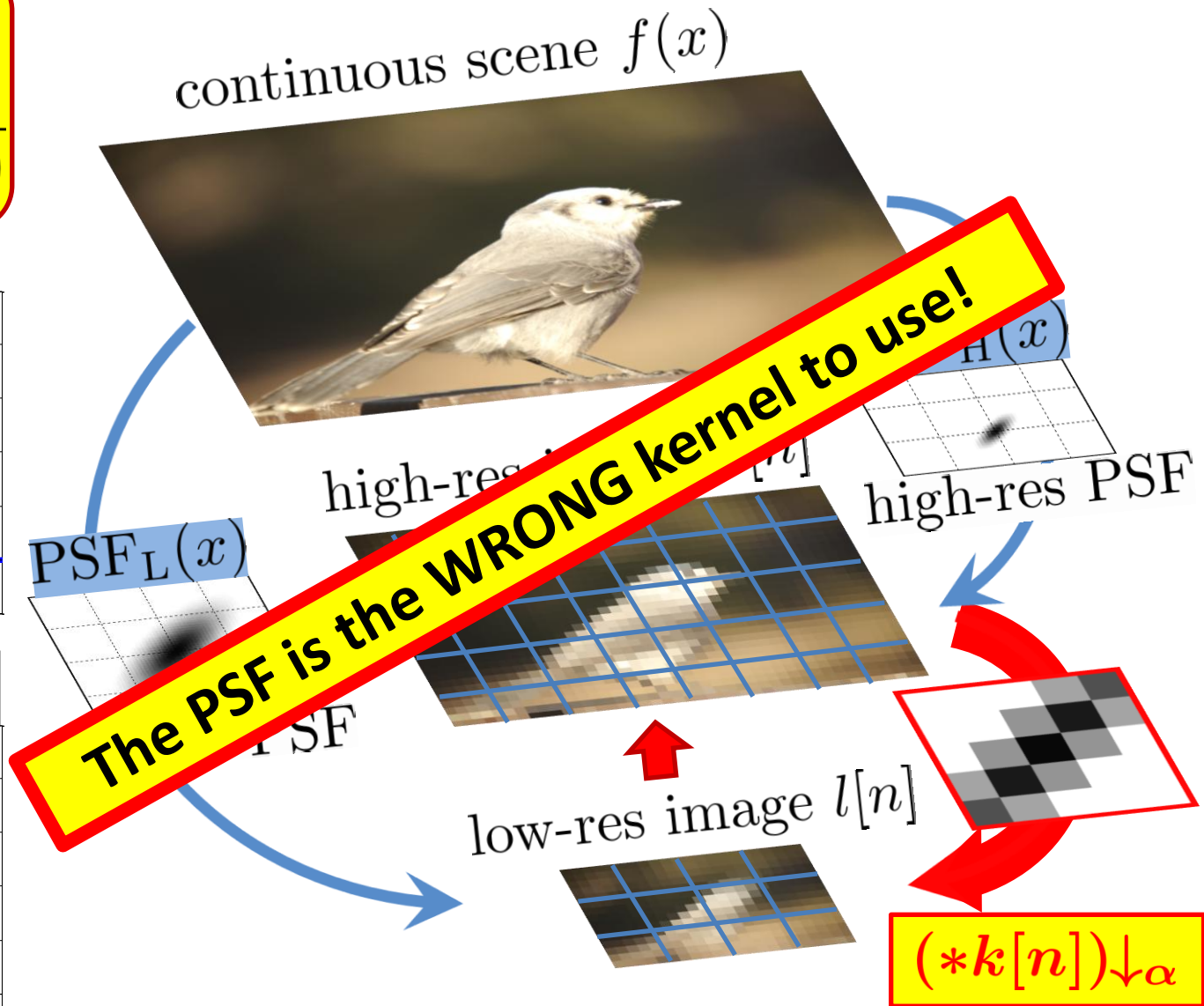
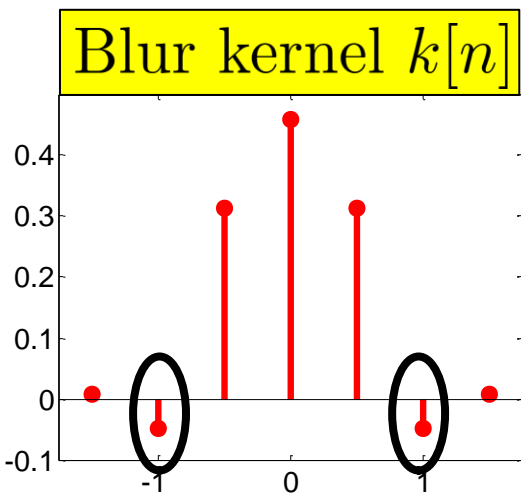
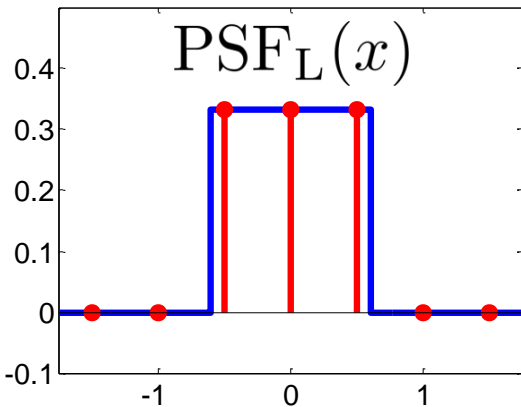
**More formally:**

$$\sum_m k[m] \text{PSF}_H\left(x - \frac{m}{\alpha}\right) = \text{PSF}_L(x)$$

# What is the Correct Blur Kernel?

Intuitively:

$$K(\omega) = \frac{\mathcal{PSF}_L(\omega)}{\mathcal{PSF}_H(\omega)}$$



# Kernel Recovery

Natural images behave like fractals

→ Small patterns recur at different scales:

– Fractal image compression

[Barnsley & Sloan `87], ...

– Single image SR

[Glasner, Bagon, Irani `09],

[Freedman & Fattal `11], ...

→ Recover the unknown  
SR blur kernel

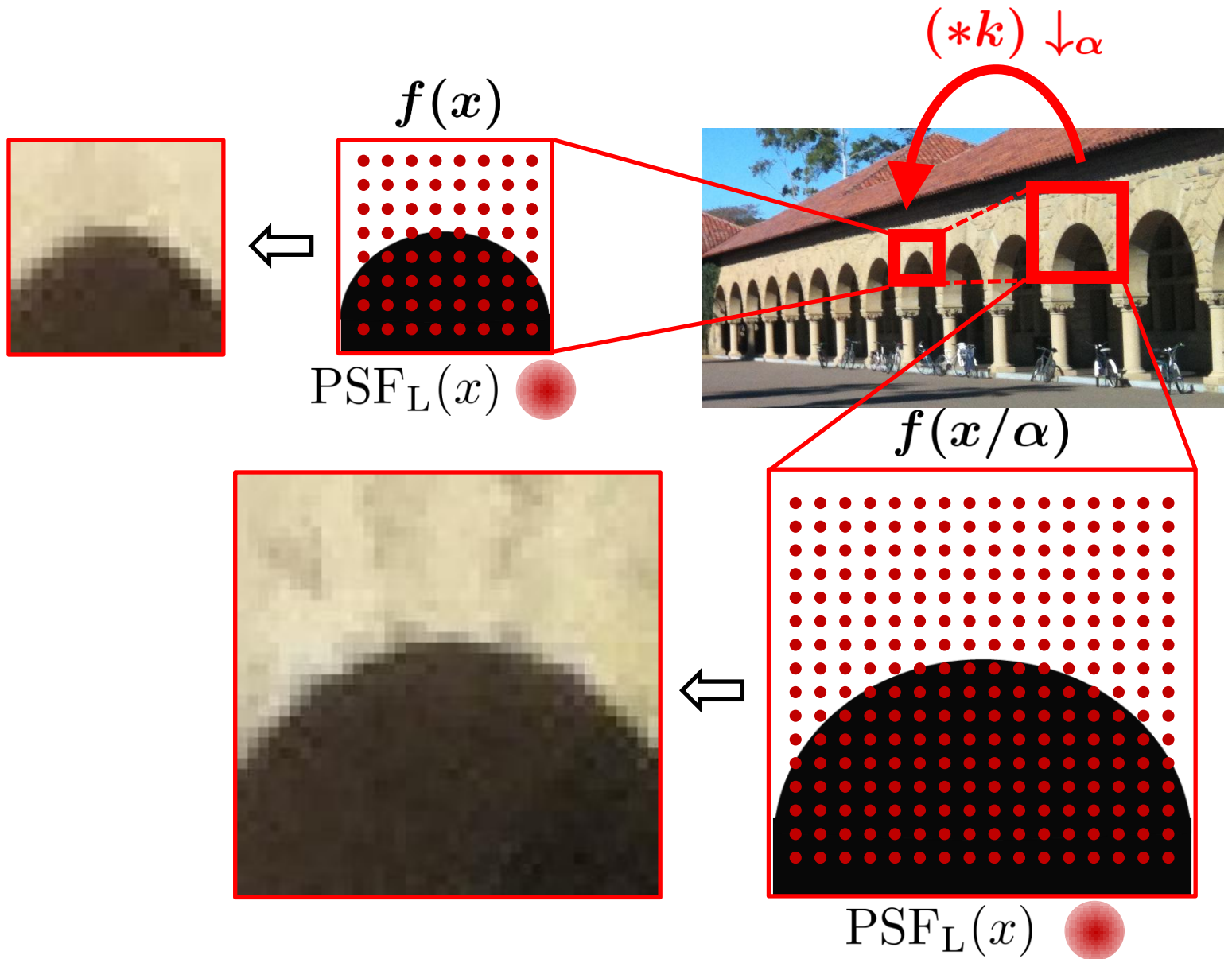
$(*k) \downarrow_{\alpha}$   
low-res image



True for most 5x5 patches  
in any natural image

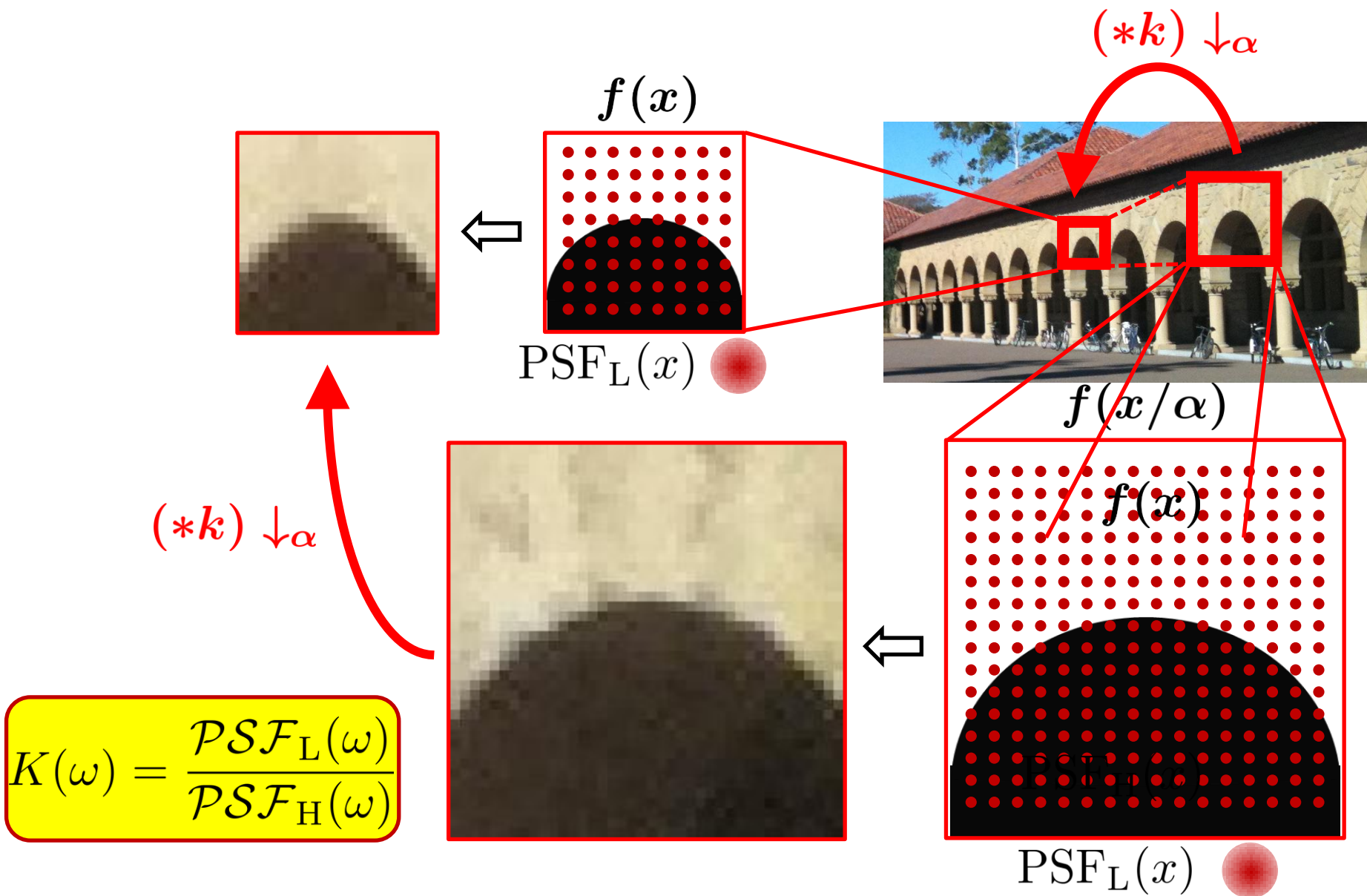
[Glasner, Bagon, Irani 2009]

# Kernel Recovery





# Kernel Recovery





# Kernel Recovery

Enough pairs allow recovering  $k$

$$q = (r * k) \downarrow_{\alpha}$$

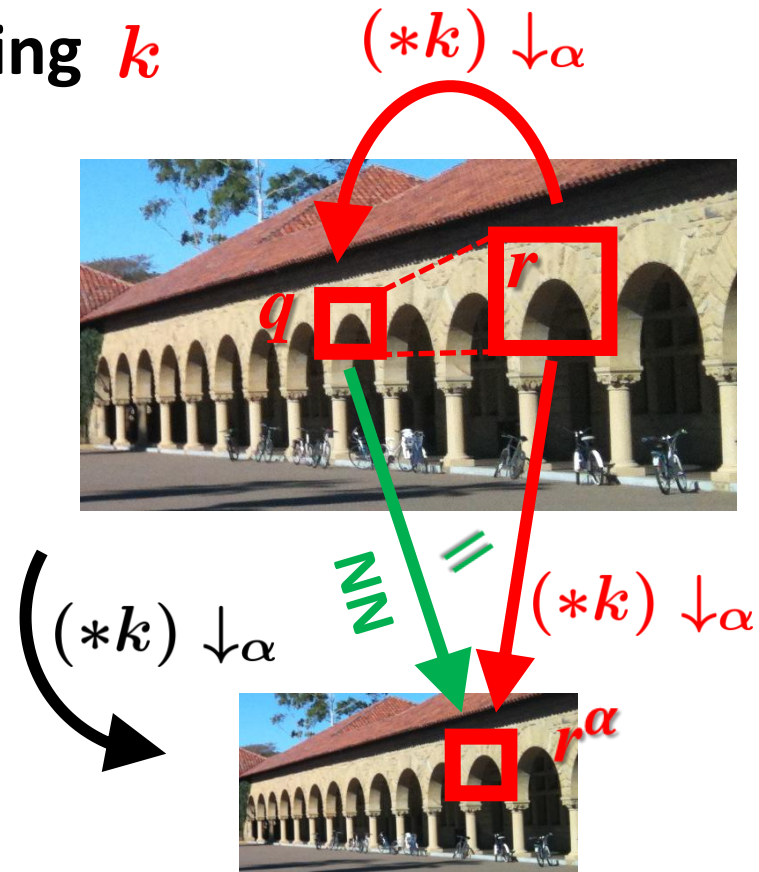
## Algorithm

Initialize  $\hat{k} = \delta$

For  $t = 1 \dots T$

1. Down-sample image with  $\hat{k}$
2. Find NNs
3. Update  $\hat{k}$  using least-squares

End

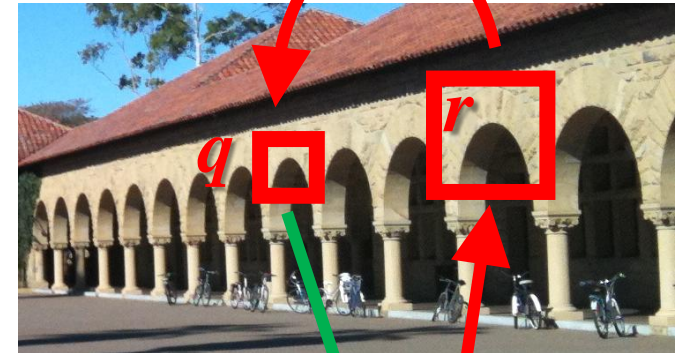


The optimal kernel  $k$  maximizes patch similarity across scales

# Kernel Recovery



$$q = (r * k) \downarrow_{\alpha}$$



Final

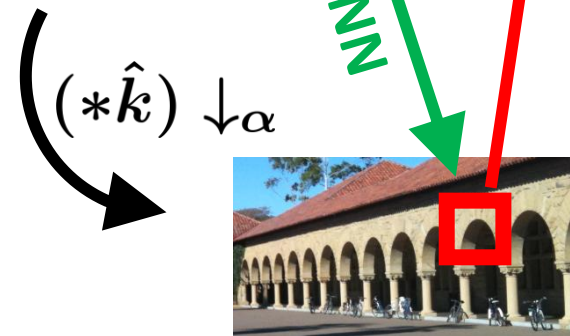
iterations

Initialize  $\hat{k} = \delta$



For  $t = 1 \dots T$

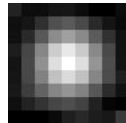
1. Down-sample image with  $\hat{k}$
2. Find NNs
3. Update  $\hat{k}$  using least-squares



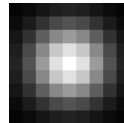
End

# Results

Low-res input image  
(generated with ground-truth kernel)



Recovered  
kernel



Ground-truth  
kernel



Default  
kernel

[1] Glasner, Bagon, Irani – ICCV 2009  
(Internal example-based SR)

[2] Zeyde, Elad, Protter – LNCS 2012  
(External example-based SR)

# SRx2 with default kernel



Default  
kernel

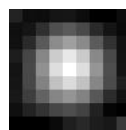
[1] Glasner, Bagon, Irani 2009



[2] Zeyde, Elad, Protter 2012



# SRx2 with Recovered kernel



Recovered  
kernel

[1] Glasner, Bagon, Irani 2009



[2] Zeyde, Elad, Protter 2012



# SRx2 with default kernel



Default kernel

[1] Glasner, Bagon, Irani 2009

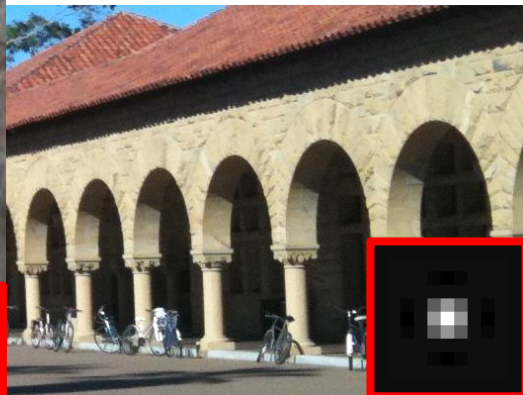
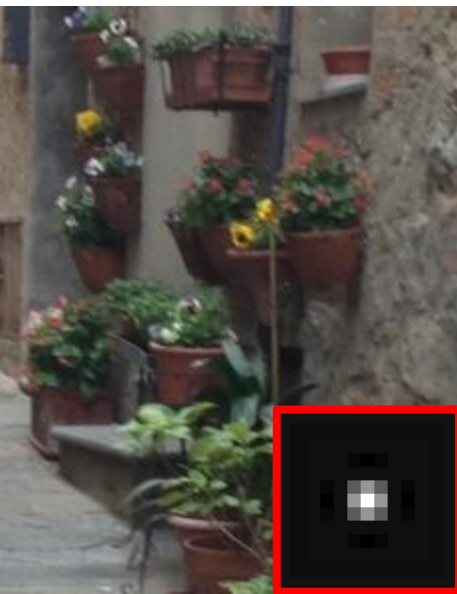
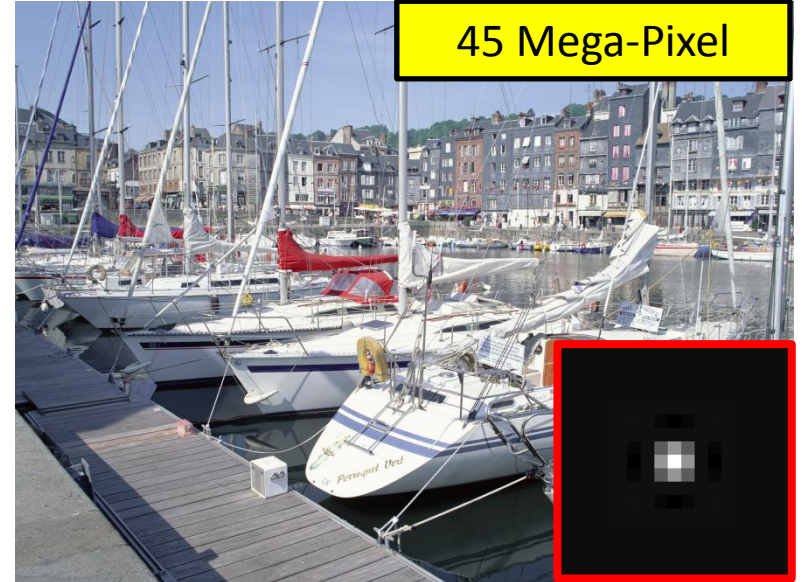


[2] Zeyde, Elad, Protter 2012



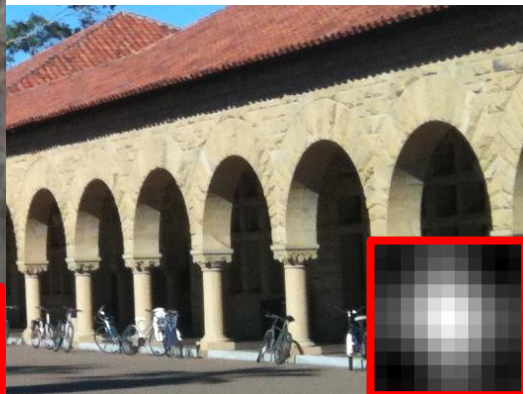
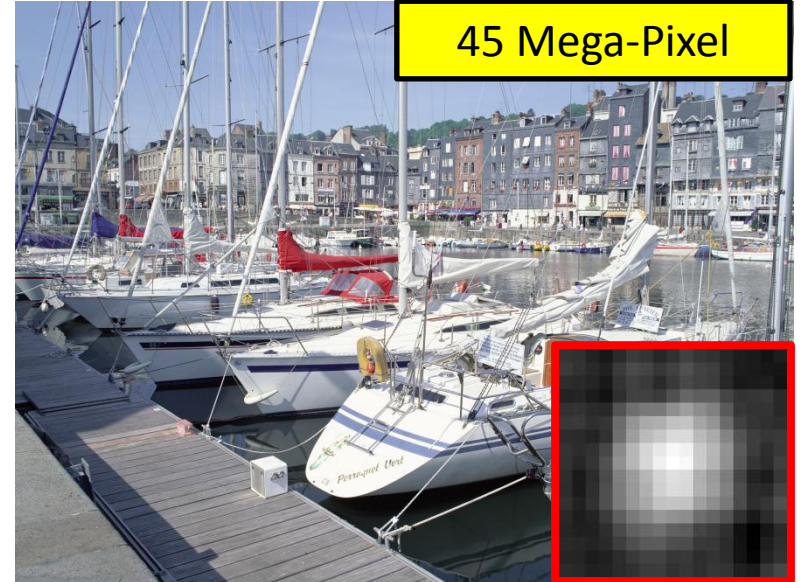


# Real (Difficult) Images





# Real (Difficult) Images



# Real (Difficult) Images

Default



45 Mega-Pixel



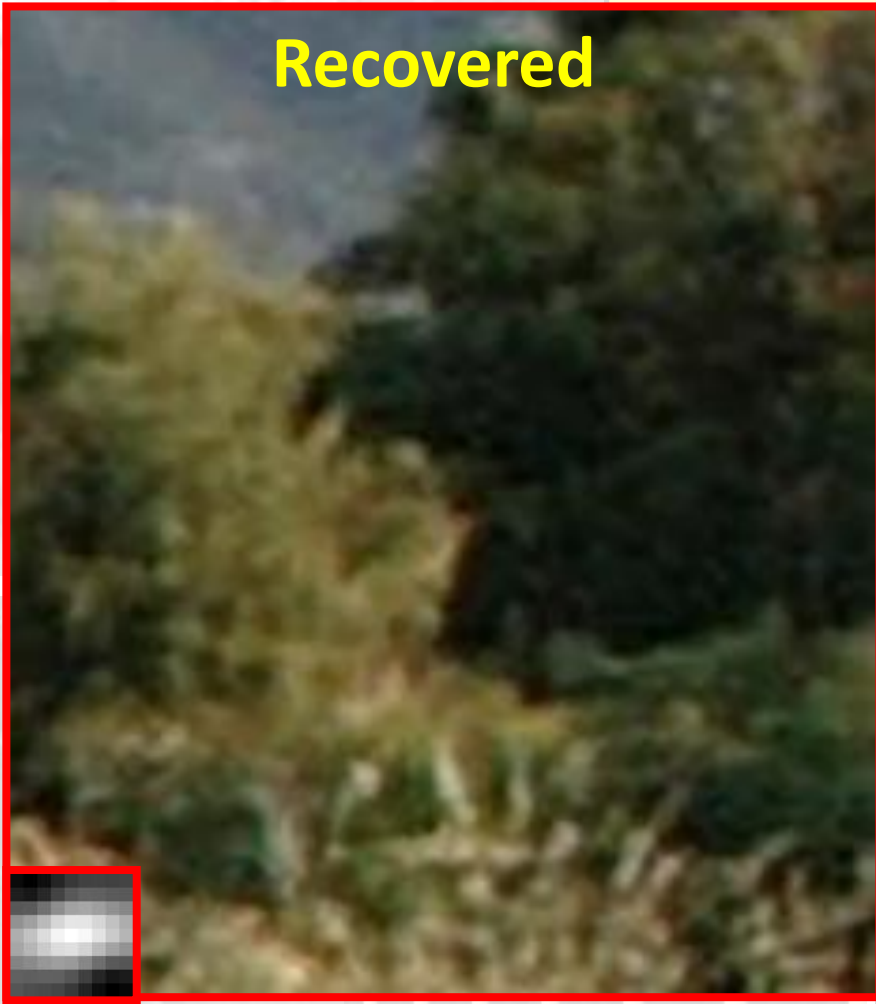
A blurry image





# Real (Difficult) Images

Recovered



45 Mega-Pixel



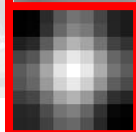
A blurry image



# Real (Difficult) Images

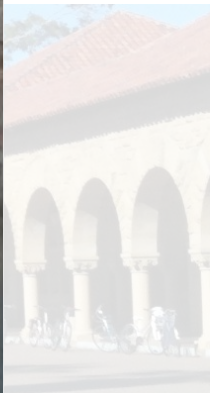


# Real (Difficult) Images

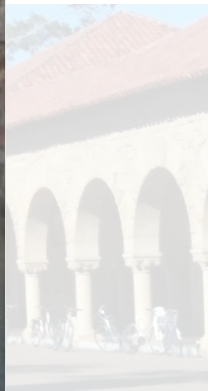
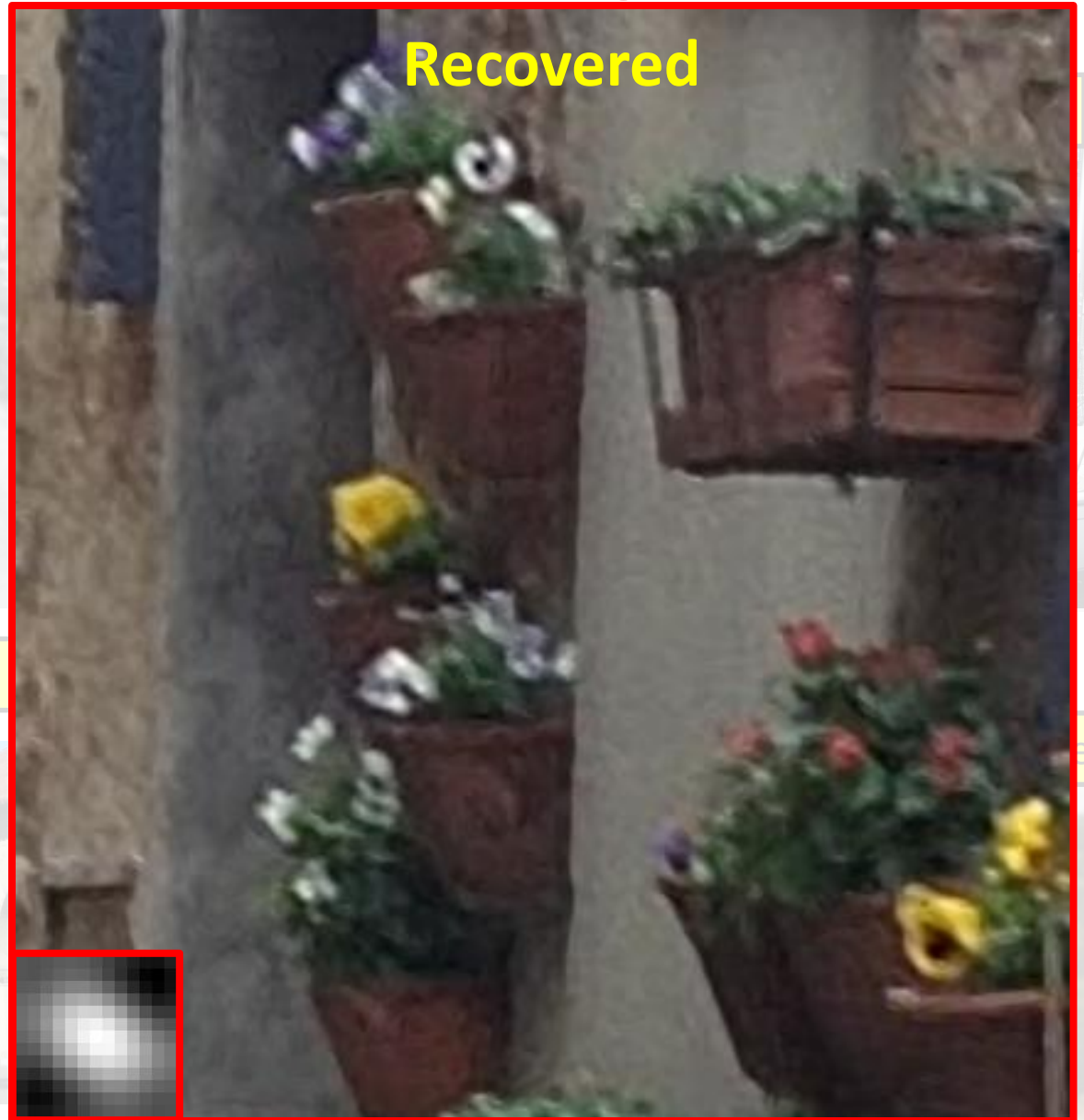




# Real (Difficult) Images



# Real (Difficult) Images





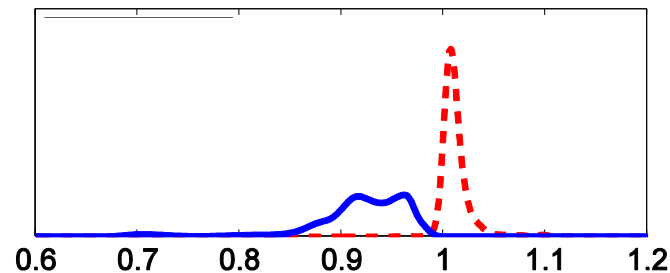
# Quantitative Results

Empirical evaluation on hundreds of images  
(with randomly generated blurs)

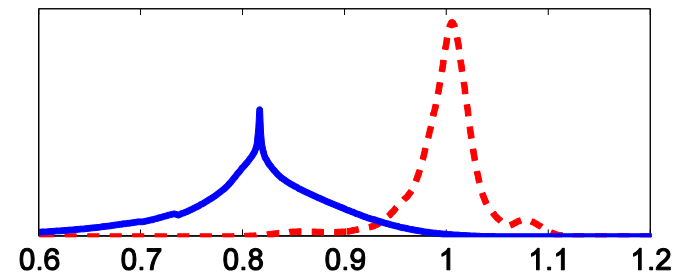
Relative error *w.r.t.* ground-truth kernel  $\frac{ERR(\text{Recovered kernel})}{ERR(\text{GT kernel})}$

Relative error *w.r.t.* default kernel  $\frac{ERR(\text{Recovered kernel})}{ERR(\text{Default kernel})}$

SR of Glasner *et al.*



SR of Zeyde *et al.*



# Conclusions

- The PSF is the **WRONG** SR blur kernel
- Recover the SR kernel from the low-res image
- Significant improvement in SR results

**THANK YOU!**